

1     **Numerical Modeling of Laminar Flame Speed and Autoignition Delay Using General**  
2                                   **Fuel-Independent Function**

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12  
13    **ABSTRACT**

14        The impact of the transport sector on climate change and carbon dioxide emissions into  
15    the atmosphere can be decreased by the utilization of biofuels and e-fuels. The chemical kinetics  
16    for calculating the combustion process of new biofuels and e-fuels is often excessively  
17    computationally demanding for numerical simulations, leading to the development and  
18    employment of combustion models, such as flamelet models. Such models require  
19    precalculated data of laminar flame speed and autoignition timing. The developed procedure in  
20    this work scrutinizes available reaction mechanisms of several fuels with the validation against  
21    existing experimental data of autoignition and laminar flame velocities, aiming for the  
22    generation of lookup databases. The autoignition of fuel/air mixtures for different conditions is  
23    pre-tabulated from nondimensional calculations of constant pressure reactor. Simultaneously,

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24 the laminar flame speed is pre-tabulated from premixed freely propagating reactors, for which  
25 calculation chemical kinetics software are applied. The ignition delay of cold flame and primary  
26 ignition was calculated using inflection point criteria implemented in the proposed method. The  
27 developed imputations method is based on the lognormal distribution for laminar flame speed  
28 in equivalence ratio direction and exponential functions for pressure, temperature, and exhaust  
29 gas recirculation directions. The laminar flame speed and autoignition databases generation  
30 procedure was demonstrated on prospective e-fuel three-oxyethylene dimethyl ether (OME-3)  
31 fuel by validating the available mechanism against the experimental data. Finally, the generated  
32 databases are implemented into the computational fluid dynamics software and verified with  
33 the detailed chemical mechanism of OME-3 fuel.

#### 34 **KEYWORDS**

35 Laminar flame speed; autoignition; flamelet model; chemical kinetics; combustion; e-fuels  
36

### 37 **1. INTRODUCTION**

38 One way to mitigate the transport sector's impact on climate change and carbon dioxide  
39 emissions into the atmosphere is the utilization of biofuels and e-fuels in the transport sector  
40 [1]. Therefore, the implementation of biofuels [2] and e-fuels [3] in conventional internal  
41 combustion engines is of great importance to accelerate the transition of the transport sector to  
42 renewable energy sources. One approach to achieving greener transport [4] and the energy  
43 sector [5] is the application of biofuels. The impact on the generation of emissions such as  
44 nitrogen oxides is still not fully explored. Therefore, numerous researches are conducted to  
45 obtain biofuel impact on emissions when they substitute conventional fuel in existing  
46 combustion systems [6]. Other modern approaches are the implementation of alternative fuels,  
47 such as ammonia and its blends with natural gas [7], synthesized kerosine from coal [8], and

48 gasoline substitutes like ethanol in passenger car engines [9] and marine engines[10], and  
49 toluene reference fuel [11].

50 There are already numerous biofuels and e-fuels, some similar and some less to  
51 conventional petrol and diesel fuels, but each with different physical properties, chemistry  
52 kinetics, and combustion characteristics [12]. In order to predict the fuel combustion under  
53 different fuel/air mixtures, loads, and temperatures, Computational Fluid Dynamics (CFD) with  
54 the chemical kinetics or combustion models are commonly employed [13]. The chemical  
55 kinetics is often too computationally demanding for numerical simulations, leading to the  
56 frequent use of combustion models, such as coherent flame models [14]. In coherent flame  
57 models, ignition delay and laminar flame velocities for different operating conditions must be  
58 precalculated in the form of a database or correlation formula [15]. The standard correlations  
59 for new biofuels and e-fuels are not accurate enough to validate their combustion process,  
60 primarily the low-temperature auto-ignition phenomenon [16]. In [17], the correlation functions  
61 between autoignition timing and flame speed propagation were developed based on the  
62 temperature gradients measured from the rapid compression.

63 Correlation functions for the autoignition of biodiesel fuels that feature ignition of fuel-  
64 air mixtures at high temperatures and their validation with the chemistry kinetic mechanisms  
65 were presented by the authors in [18], where the excellent agreement between the previously  
66 published mechanism was achieved. The dependency of autoignition timing and pollutant  
67 emissions results was demonstrated in [19], where the convenient diesel fuels with some  
68 percentage of biodiesel were observed at high-temperature conditions. The investigation results  
69 are that the rise in the ambient temperature lowers the ignition delay for all diesel fuel, which  
70 was expected. Recent publications have also investigated the investigation of biodiesel fuels  
71 produced by different sources [20]. For example, the autoignition delay of microalgae biodiesel  
72 blends was investigated numerically to determine combustion efficiency and pollutant

73 emissions [21]. Additionally, an experimental autoignition investigation of biodiesel produced  
74 from the plant oil and its impact on the combustion process inside a compression ignition engine  
75 was observed [22]. The results showed that the biodiesel blend at 20% of the content exhibited  
76 better combustion performance and emission characteristics than other blend proportions.

77 In [23], the authors performed an experimental optical study of biodiesel ignition delay,  
78 where the correlation between autoignition timing and combustion process was demonstrated.  
79 A similar approach for determining the influence of pollutant concentrations of nitrogen oxides  
80 and carbon monoxide on autoignition timing under different exhaust gas recirculation (EGR)  
81 mass fractions was examined by the authors [24], where the diesel fuel with a small share of  
82 biodiesel was used. For the internal combustion engine operating conditions, a numerical  
83 method named spherically expanded flames was used to determine the autoignition and laminar  
84 flame speed propagation for a different share of e-fuel (dimethyl-ether), air, and helium [25].  
85 The simulation results adequately captured the physics of unsteady flame propagation,  
86 autoignition, and the controlling reactions, but not at the early ignition stages.

87 Lately, the penetration of machine learning techniques has accelerated enormously in all  
88 science areas, so in this area too. Rahnama et al. [26] proposed the machine learning neural  
89 network for fuel consumption reduction in internal combustion engines, where the start of  
90 injection and its influence on autoignition timing was observed. Deep neural networks for  
91 internal combustion engines were also employed to determine emissions from the biodiesel  
92 combustion process [27]. In [28], the authors published the results of dual-fuel autoignition,  
93 which were predicted by the machine learning technique. The sensitivity analysis showed that  
94 the fuel ratio between the primary and secondary fuels has the most significant effect on dual-  
95 fuel ignition. Furthermore, an exciting approach, similar to the developed procedure in this  
96 work, was published by the authors of [29], where the calculation of the autoignition and  
97 laminar flame speed was modeled by ignition to propagation reduced scheme, which was

98 upgraded to additionally calculate the autoignition timing. Another approach that aims to obtain  
99 laminar flame speed with general formula is presented in [30]. The authors introduced a term  
100 that depends on polynomial, exponential factors, with additional constant defined from the  
101 precomputed database. Additionally, the same procedure was applied for obtaining  
102 ethanol/gasoline blends databases, where high accuracy in correlation is achieved [31]. Other  
103 researchers tend to determine laminar flame speed correlations for a single fuel. In [32], the  
104 authors proposed correlation functions for surrogate gasoline fuels as an exponential function  
105 in temperature and pressure direction. An exceptional scientific contribution was conducted to  
106 developing correlation functions of hydrogen fuel for spark ignition operating conditions [33].  
107 Furthermore, additional research has been undertaken to develop correlation functions capable  
108 of describing hydrogen mixture with gasoline [34] and methanol [35] for combustion inside  
109 spark-ignition engines.

110 In this work, the effects of complex chemistry kinetics are reproduced by developing  
111 efficient database creation consisting of the relevant ignition data used by existing combustion  
112 models. In the pre-processing stage, available reaction mechanisms of several fuels were  
113 investigated and validated against existing experimental data of autoignition and laminar flame  
114 velocities. The autoignition of fuel/air mixtures for different conditions is pre-tabulated from  
115 nondimensional constant pressure reactor calculation. At the same time, the laminar flame  
116 speed is pre-tabulated from premixed freely propagating reactors, for which the LOGEsoft™  
117 and Cantera open-source software were used. The ignition delay of cold flame and main ignition  
118 was calculated using the inflection point criteria presented in [35] and implemented in the  
119 proposed method. The data imputation and extrapolation method was developed as a general  
120 fuel-independent function. The nonlinear least squares algorithm was employed to fill the  
121 unsuccessfully calculated points of databases in the post-processing.

122 In this work, the novel general, fuel-independent procedure is developed and implemented into  
123 CFD software based on the lognormal distribution for laminar flame speed in equivalence ratio  
124 direction and exponential functions for pressure, temperature, and exhaust gas recirculation  
125 directions. Three parameters are used to determine the dependence of the laminar flame speed  
126 or autoignition results on pressure and equivalence ratio directions. Additionally, the method is  
127 also applicable to dual-fuel combustion. The ignition delay and laminar flame speed values of  
128 fuel blends are described with the additional parameter of the fuel composition. Finally, the  
129 database implementation is verified with the detailed chemical mechanism of complex internal  
130 combustion operating case in computational fluid dynamics and validated with experimental  
131 data.

132

## 133 **2. MATHEMATICAL MODEL**

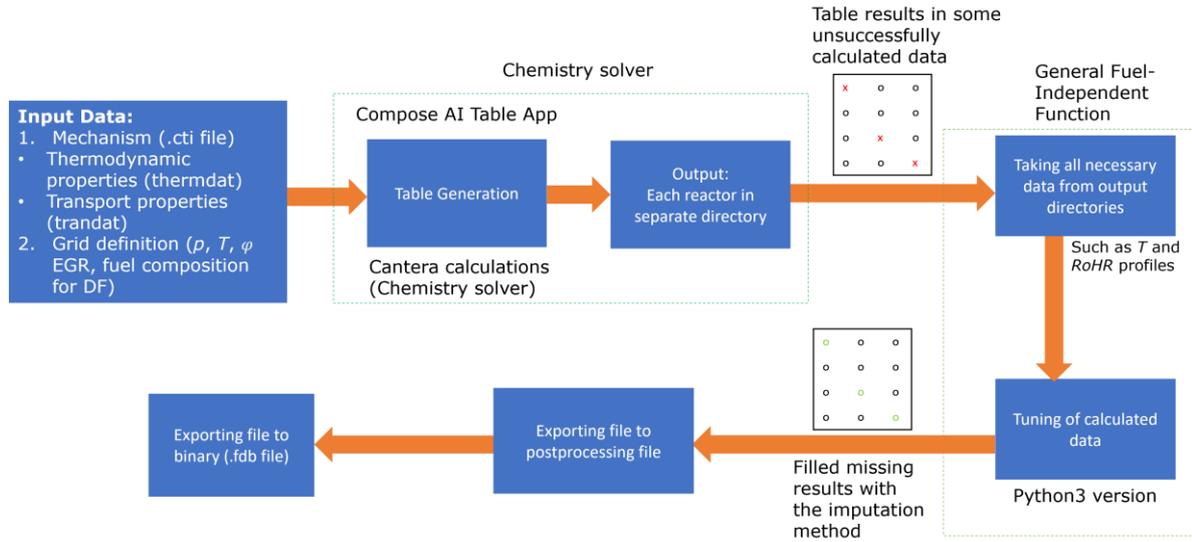
134 In this section, the mathematical model for calculating the correlation function and models  
135 used in the validation and verification are presented. For chemistry calculation, commercial  
136 LOGEsoft™ and Cantera open-source software were used, while for CFD simulation AVL  
137 FIRE™ was used.

138

### 139 **2.1. Laminar flame speed**

140 For the definition of the correlation function of the laminar flame speed points, firstly, the  
141 calculation on chemistry solvers was performed. The chemistry solver calculations were defined  
142 with the four-dimensional grid: temperature, pressure, equivalence ratio, and EGR. The  
143 calculations were performed on premixed freely propagating reactors, where each combination of  
144 four previously mentioned parameters was calculated as a separated reactor. The raw calculated  
145 data were sorted in the five-dimensional matrix, on which the correlation function is performed.

146 Figure 1 shows the procedure of the developed method for the generation of a laminar flame speed  
 147 database for the coherent flame models.



148  
 149 Figure 1 Flowchart of the developed procedure for generation of laminar flame speed and  
 150 autoignition databases

152 The correlation function was tuned for calculated data, which was defined as the lognormal  
 153 distribution for equivalence ratio ( $\varphi$ ) and as the exponential function for the pressure ( $p$ ) direction.

154 The tuning equation has the following form:

$$S_L(p, \varphi) = S_{L,ref} \left[ \frac{1}{\varphi\sigma\sqrt{2\pi}} \exp\left(-\frac{(\ln \varphi - \mu)^2}{2\sigma^2}\right) \right] \left(\frac{p}{p_{ref}}\right)^\beta \quad (1)$$

156 where  $\mu$  and  $\sigma$  are two tuning parameters that are calculated for each combination of the  
 157 temperature and EGR. For the calculation of  $\mu$  and  $\sigma$  parameters that have the lowest disagreement  
 158 with the raw computed data, the nonlinear least-squares method was employed with the  
 159 Levenberg-Marquardt algorithm.  $p_{ref}$  is reference pressure of 0.1 MPa, while  $S_{L,ref}$  is referent  
 160 laminar flame speed at selected calculated point, which was in this case at equivalence ratio 1, and  
 161 pressure 0.1 MPa. The algorithm was based on SciPy open-source package and its function

162 scipy.optimize.least\_squares that accounts for the optimized parameters of general function for  
163 each temperature point. In order to obtain the optimized parameters, the objective function is  
164 defined as:

165

$$f_{S_L} = \min \sum_{i=1}^m [S_{L_i} - S_L(p_i, \varphi_i)]^2 \quad (2)$$

166 where  $S_{L_i}$  is the calculated laminar flame speed from the chemistry solver, and  $m$  is the number of  
167 points used for obtaining the formula of laminar flame speed. The objective function is  
168 approximated by the linearization in each iteration step. The  $\varphi$  is changed with the estimation  $\varphi +$   
169  $\delta$ , and to determine  $\delta$  the following term has to be calculated:

170

$$f_{S_L} \approx S_L(p_i, \varphi_i + \delta) + \frac{\partial S_L(p_i, \varphi_i)}{\partial \varphi} \delta \quad (3)$$

171

## 172 **2.2. Autoignition timing**

173 For the definition of the correlation function of the autoignition points, firstly, the calculation  
174 on chemistry solvers was performed. The chemistry solver calculations were also defined with the  
175 four-dimensional grid, where the parameters were temperature, pressure, equivalence ratio, and  
176 EGR, the same as in the laminar flame speed calculations. The calculations were performed on  
177 nondimensional, perfectly stirred reactors, where each combination of four previously mentioned  
178 parameters was calculated as a separated reactor. The raw calculated data were sorted in the eight-  
179 dimensional matrix, where the four additional output parameters were autoignition timing, cold  
180 flame autoignition timing, released heat, and heat released by cold flame. The procedure of the  
181 developed method for generating the autoignition ( $\tau$ ) database is similar to the laminar flame speed  
182 database for the coherent flame models.

183

$$\tau(p, \varphi) = \tau_{ref} \left( \frac{p}{p_{ref}} \right)^\alpha (\varphi)^\beta \quad (4)$$

184 where  $\alpha$  and  $\beta$  are two tuning parameters calculated for each combination of the temperature and  
185 EGR. For the calculation of  $\alpha$  and  $\beta$  parameters that have the lowest disagreement with the raw  
186 calculated data, the nonlinear least-squares method was employed with the Levenberg-Marquardt  
187 algorithm. The objective function is defined as

188

$$f_\tau = \min \sum_{i=1}^m [\tau_i - \tau(p_i, \varphi_i)]^2 \quad (5)$$

189 Where the objective function is approximated by the linearization in each iteration step. The  $\varphi$  is  
190 changed with the estimation  $\varphi + \delta$ , and to determine  $\delta$  the following term has to be calculated:

191

$$f_\tau \approx \tau(p_i, \varphi_i + \delta) + \frac{\partial \tau(p_i, \varphi_i)}{\partial \varphi} \delta \quad (6)$$

192 As in the case of the laminar flame speed algorithm was set to bisquare robust regression.

193

### 194 **2.3. Coherent flame model – ECFM-3Z**

195 An alternative to modeling combustion via chemical kinetics is using a coherent flame  
196 model suitable for simulating combustion inside diesel engines. One of such models is the  
197 extended coherent flame model in 3 zones (ECFM-3Z). It has a decoupled treatment of chemistry  
198 and turbulence [36].

199 In the model, the following equation is solved for the flame surface density  $\Sigma$ :

200

$$\frac{\partial \Sigma}{\partial t} + \frac{\partial}{\partial x_j} (\bar{u}_j \Sigma) - \frac{\partial}{\partial x_j} \left( \frac{\nu_t}{Sc_t} \frac{\partial \Sigma}{\partial x_j} \right) = S_\Sigma \quad (7)$$

201 where  $t$  is time,  $x_j$  are Cartesian coordinates,  $\bar{u}_j$  is averaged velocity in Cartesian coordinates,  $\nu_t$   
 202 is the turbulent kinematic viscosity,  $Sc$  is unidimensional Schmidt number, and  $S_\Sigma$  is the source  
 203 term in which laminar flame speed contribution is added through three phenomena, flame  
 204 propagation, flame destruction and flame straining. In the model, transport equations for the  
 205 following species are solved: O<sub>2</sub>, N<sub>2</sub>, NO, CO<sub>2</sub>, CO, H<sub>2</sub>, H<sub>2</sub>O, O, H, N, OH:  
 206

$$\frac{\partial \bar{\rho} \tilde{Y}_X}{\partial t} + \frac{\partial \bar{\rho} \tilde{u}_i \tilde{Y}_X}{\partial x_i} = \frac{\partial}{\partial x_i} \left( \left( \frac{\mu}{Sc} + \frac{\mu_t}{Sc_t} \right) \frac{\partial \tilde{Y}_X}{\partial x_i} \right) + \bar{\omega}_X \quad (8)$$

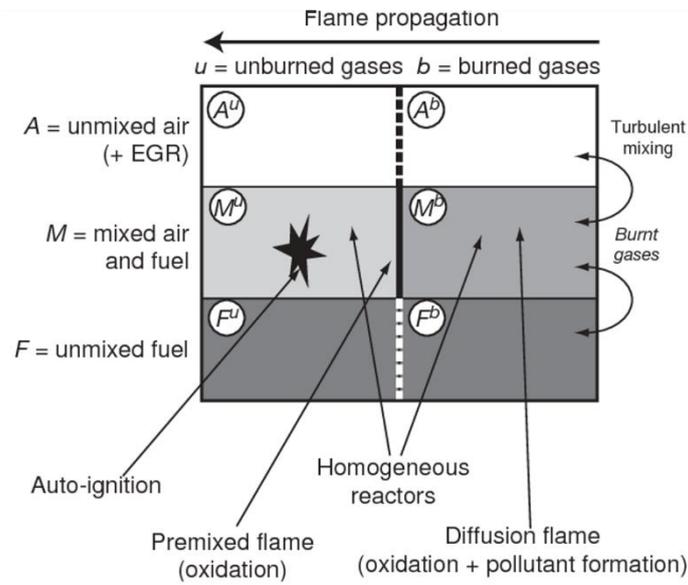
207 Where  $\bar{\omega}_X$  is the average combustion source term and  $\tilde{Y}_X$  is the average mass fraction of species  
 208  $X$ , while  $\bar{\rho}$  is averaged density. The fuel is divided into two parts: the unburned ( $\tilde{Y}_{Fu}^u$ ) and burned  
 209 ( $\tilde{Y}_{Fu}^b$ ) fuel. For both of them, additional transport equations are solved:  
 210

$$\frac{\partial \bar{\rho} \tilde{Y}_{Fu}^u}{\partial t} + \frac{\partial \bar{\rho} \tilde{u}_i \tilde{Y}_{Fu}^u}{\partial x_i} = \frac{\partial}{\partial x_i} \left( \left( \frac{\mu}{Sc} + \frac{\mu_t}{Sc_t} \right) \frac{\partial \tilde{Y}_{Fu}^u}{\partial x_i} \right) + \bar{\rho} \tilde{S}_{Fu}^u + \bar{\omega}_{Fu}^u - \bar{\omega}_{Fu}^{u \rightarrow b} \quad (9)$$

$$\frac{\partial \bar{\rho} \tilde{Y}_{Fu}^b}{\partial t} + \frac{\partial \bar{\rho} \tilde{u}_i \tilde{Y}_{Fu}^b}{\partial x_i} = \frac{\partial}{\partial x_i} \left( \left( \frac{\mu}{Sc} + \frac{\mu_t}{Sc_t} \right) \frac{\partial \tilde{Y}_{Fu}^b}{\partial x_i} \right) + \bar{\rho} \tilde{S}_{Fu}^b + \bar{\omega}_{Fu}^b + \bar{\omega}_{Fu}^{u \rightarrow b} \quad (10)$$

211 where  $\tilde{S}_{Fu}^u$  is a source term representing fuel evaporation.  $\bar{\omega}_{Fu}^u$  and  $\bar{\omega}_{Fu}^b$  represent oxidation of  
 212 (un)burned fuel, while  $\bar{\omega}_{Fu}^{u \rightarrow b}$  represents fuel mass transfers between various zones.  $\mu$  and  $\mu_t$  are  
 213 laminar and turbulent dynamic viscosity.

214 The combustion area can be divided into three zones: a pure fuel zone, a pure air plus possible  
 215 EGR zone, and mixed air and fuel zone. The model describes autoignition and premixed and  
 216 diffusion flames. A schematic showing these zones is shown in Figure 2 [37].  
 217



219

220

Figure 2 Schematic of the ECFM-3Z model cell [37]

221

### 222 3. VALIDATION

223

224

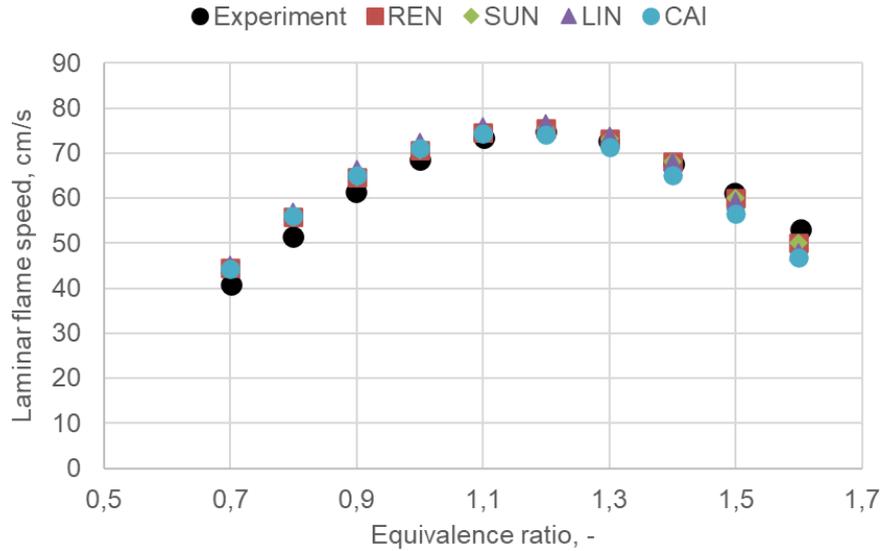
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For the validation of the calculated data from chemistry solvers, four mechanisms of e-fuel OME-3 were compared with the experimental data: Cai et al. [16], Ren et al. [38], Sun et al. [39], and Lin et al. [40]. Figure 3 shows the calculated laminar flame results at a pressure of 0.1013 MPa and temperature of 408 K, and with four previously mentioned chemical mechanisms, where good agreement was achieved with all data.



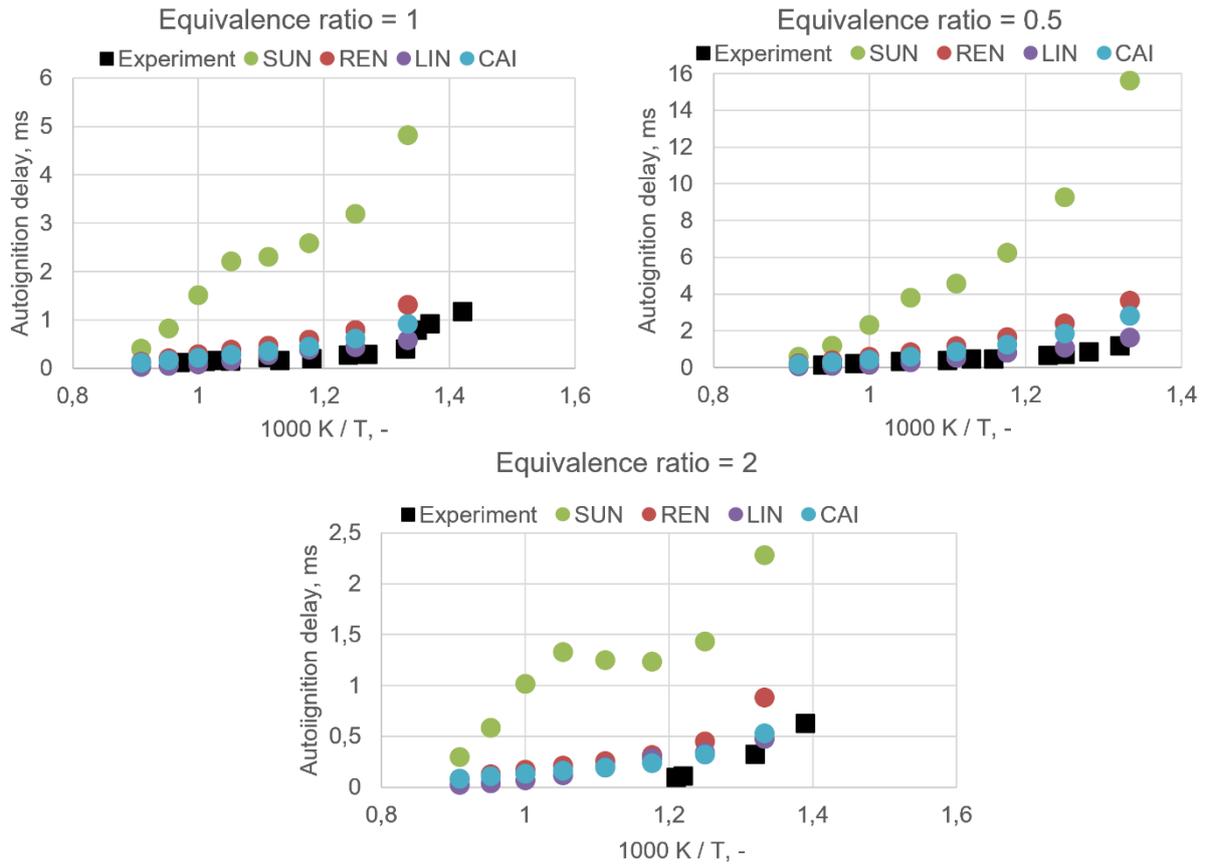
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230 Figure 3 Comparison of calculated laminar flame speed with four chemical mechanisms and  
 231 experimental data at 0.1013 MPa and 408 K

232

233 For the exact mechanism, the validation of results was performed on the autoignition results, where  
 234 the best agreement with experimental data was achieved with the Lin et al. mechanism. The  
 235 autoignition results were performed in Figure 4, where the results are shown at the pressure of 2  
 236 MPa for equivalence ratio values of 0.5, 1.0, and 2.0. The experimental autoignition results are  
 237 taken from [16]. According to the performed validation, the Cai et al. chemical mechanism was  
 238 selected to further investigate the correlation function since it features the highest number of  
 239 chemical reactions and chemical species.

240



241

242 Figure 4 Comparison of calculated autoignition data with four chemical mechanisms and  
 243 experimental data at 2 MPa for equivalence ratios: 0.5, 1.0 and 2.0

244

#### 245 4. NUMERICAL SETUP

246 This chapter presents the numerical setup of the verification case for generated laminar  
 247 flame speed and autoignition tables of OME-3 fuel. The verification case was performed on  
 248 Volvo I5D engine, for which the detailed description of mesh dependency is available in [13].  
 249 The engine and injector data are shown in Table 1.

250

251

Table 1 Engine and injector specifications

Engine data	
Bore	81 mm

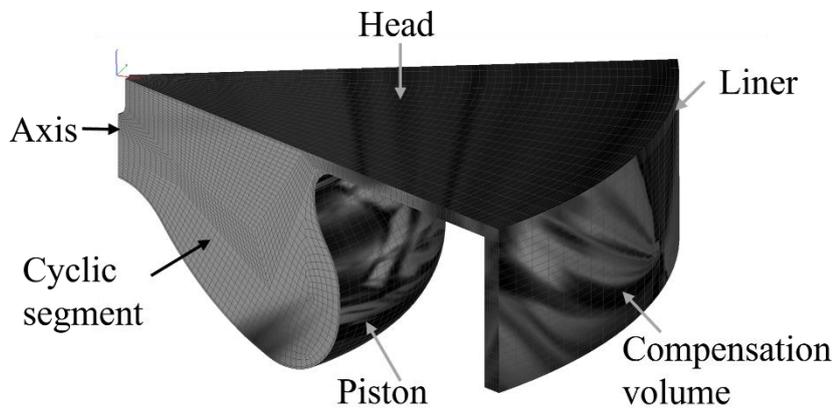
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Stroke	93.15 mm
Connecting rod length	147 mm
Compression ratio	16.5 : 1
Displacement	2.4 dm <sup>3</sup>
Number of cylinders	5
<b>Injector data</b>	
Number of nozzle holes	7
Spray cone angle	145°
Flow rate (at 100 bar Δp)	440 cm <sup>3</sup> / 30 s
The shape of the nozzle dome	Micro Sac

253

254 The calculation of a moving computational mesh shown in Figure 5 was generated with the  
 255 defined boundary selections. Due to the cyclic symmetry, the computation mesh is the cylinder  
 256 part that features a single nozzle hole. Mesh details, like volume and number of cells, are given  
 257 in Table 2. In Table 3, the boundary conditions of the engine operating cases are shown.

258



259

260 Figure 5 Boundary selections of the computational mesh

261

262 Table 2 Mesh details

	<b>Top Dead Centre</b>	<b>Bottom Dead Centre</b>
<b>Volume, cm<sup>3</sup></b>	4.67	75.88
<b>Number of cells</b>	54 663	112 854

263

264

265

Table 3 Boundary conditions for the verification operating case

<b>Face selection</b>	<b>Boundary Condition</b>
<b>Piston</b>	Type: Wall Temperature: 473 K
<b>Liner</b>	Type: Wall Temperature: 423 K
<b>Axis</b>	Type: Symmetry
<b>Segment</b>	Type: Inlet/Outlet
<b>Compensation volume</b>	Type: Wall, Mesh movement
<b>Head</b>	Type: Wall Temperature: 443 K

266

267 In Table 4, injection parameters for two observed operating cases are shown. Two cases that  
 268 feature single and multi-injection strategies are selected in order to prove the capability of valid  
 269 autoignition and combustion process modeling for both modeling strategies.

270

271

Table 4 Injection parameters for the verification operating cases

	<b>Multi injection</b>	<b>Single injection</b>
<b>Injected mass</b>	0.4, 0.4, 5.8, 0.8 mg	4.12 mg
<b>Injection timing</b>	683.9 - 740.7 °CA	718.2 - 731.3 °CA

272

273 For the time discretization, an automatic time step was used, where the maximum value of the  
 274 local CFL number was set to 1. For the calculation of the spray process, the Euler Lagrangian  
 275 model was used [41], with the Wave breakup model [42] and Abramzon evaporation model [43].  
 276 The CFD verification simulations are performed using the AVL AST software package, which has  
 277 implemented the ECFM-3Z model and detail chemistry solvers. In Table 5, the grid definition of  
 278 generated lookup databases for CFD implementation is given.

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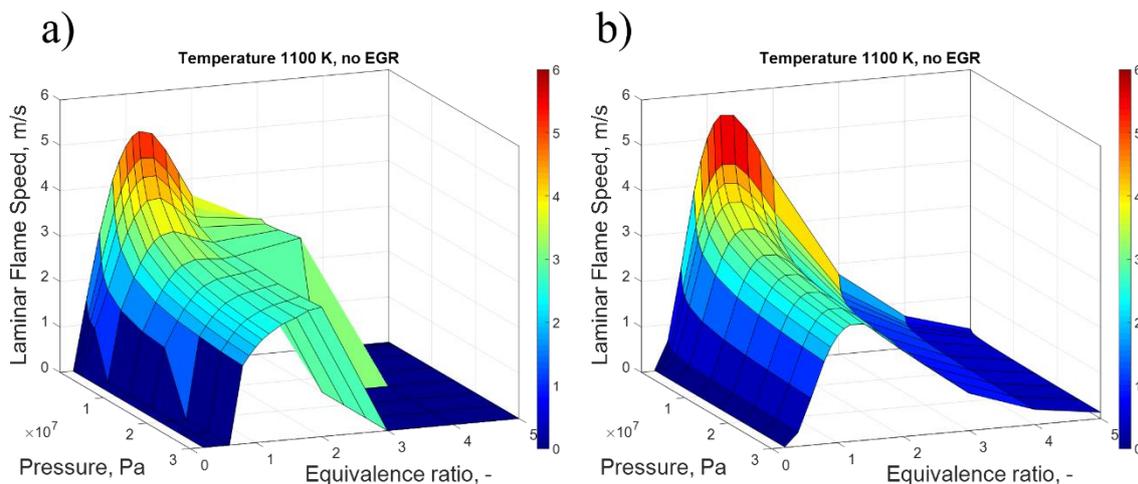
Table 5 Grid definition for laminar flame speed and autoignition timing databases

Laminar flame speed	Grid points
Temperature, K	300, 400, 500, 600, 700, 800, 900, 1000, 1100, 1250
Pressure, MPa	0.1, 0.2, 0.5, 1, 2, 5, 10, 15, 20, 25, 30
Equivalence ratio, -	0.2, 0.4, 0.6, 0.8, 0.9, 1, 1.1, 1.2, 1.4, 1.6, 1.8, 2, 3, 4, 5
EGR, -	0, 0.2, 0.4, 0.6
Autoignition	Grid points
Temperature, K	600, 620, ..., 740, 760, 800, 840, ..., 1400, 1440, 1500
Pressure, MPa	0.1, 0.2, 0.5, 1, 2, 5, 10, 15, 20, 25, 30
Equivalence ratio, -	0.2, 0.4, 0.6, 0.8, 0.9, 1, 1.1, 1.2, 1.4, 1.6, 1.8, 2, 3, 4, 5
EGR, -	0, 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8

284

285 **5. RESULTS AND DISCUSSION**

286 In this section, the results of the developed correlation functions and calculated data were  
 287 compared on three-dimensional and two-dimensional diagrams. Figure 6 shows the calculated and  
 288 tuned laminar flame speed results with the correlation function in Equation (1) at 1100 K with Cai  
 289 et al. chemical mechanism. The a) diagram of Figure 6 shows the surface of raw data calculated  
 290 from the chemistry solver, which is tuned with the correlation function, and where the results at  
 291 the b) diagram of Figure 6 are obtained.



292

293 Figure 6 Calculated chemistry solver results (a) and laminar flame speed results with the

294

correlation functions (b) at 1100K

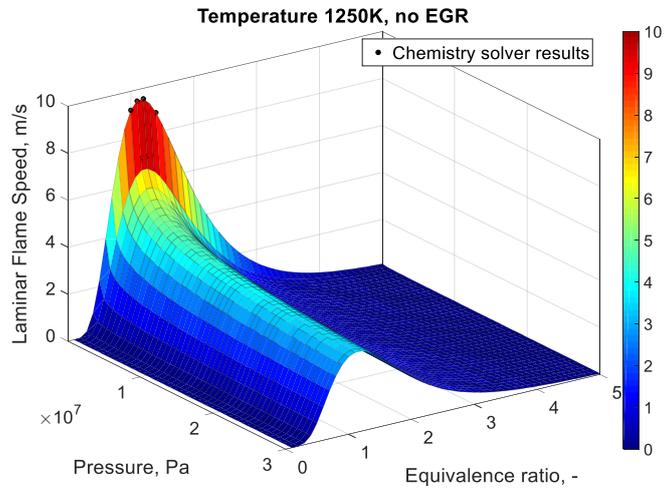
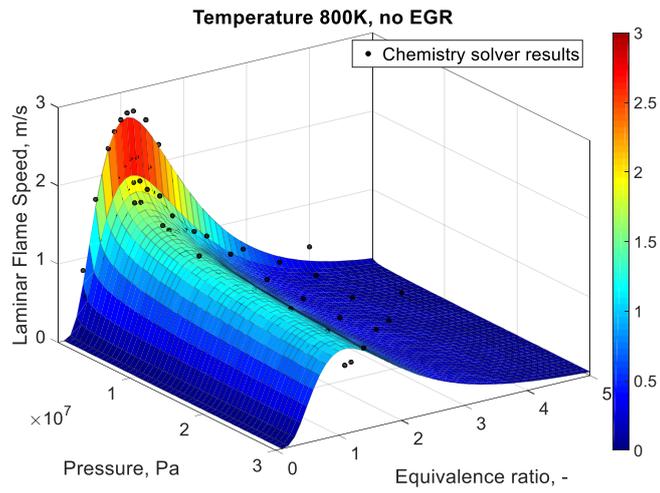
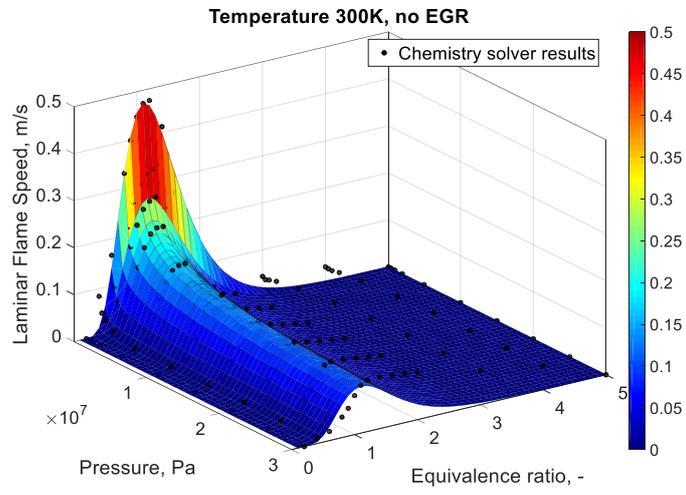
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296 Figure 8 shows the calculated results from the chemistry solver used as input to obtain the shape  
297 of laminar flame speed data and the shape obtained by the correlation function procedure on four  
298 parameters: temperature, equivalence ratio, pressure, and EGR mass fraction. The calculated  
299 laminar flame speed data is shown as the black dots, while the surface shows the results with the  
300 correlation function in Equation (1). From Figure 8 **Pogreška! Izvor reference nije pronađen.**, a  
301 good trend is achieved between calculated results and the results obtained from the general  
302 function approach. For the highest temperature, 1250 K, only 6 points are obtained from chemistry  
303 solver reactions, compared to the lower temperatures where the chemistry solver is more stable.  
304 The general function approach shows a robust extrapolation solution for such cases since it only  
305 needs 3 points to determine the whole laminar flame speed shape in pressure and equivalence ratio  
306 directions. In Figure 8, the same results for different pressure values. It can be seen that the  
307 agreement between the general function approach and calculated data using the conventional  
308 Gülder approach for extrapolation [44] is better for the lean mixtures and around the stoichiometric  
309 equivalence ratio. At the same time, a more significant discrepancy was achieved for the fuel-rich  
310 region.

311 Figure 9 shows the same results as in Figure 7 for temperature of 800 K, at different pressure  
312 values. Additionally, the number of successfully calculated data from the chemistry solver (red  
313 circles) is reduced with pressure and equivalence ratio increase. Nevertheless, as shown, the  
314 general function method shows good robustness with fewer obtained points. Additionally, the  
315 method was also validated against calculated laminar flame speeds at different EGR values in  
316 Figure 10. With increased EGR, a more significant discrepancy with chemistry solver data is  
317 obtained, which has unexpectedly high values in fuel rich regions. Such high values can also be  
318 attributed to the drawback of a chemical mechanism not intended to calculate the laminar flame  
319 speed for such conditions or to chemistry solver converging deficiency.

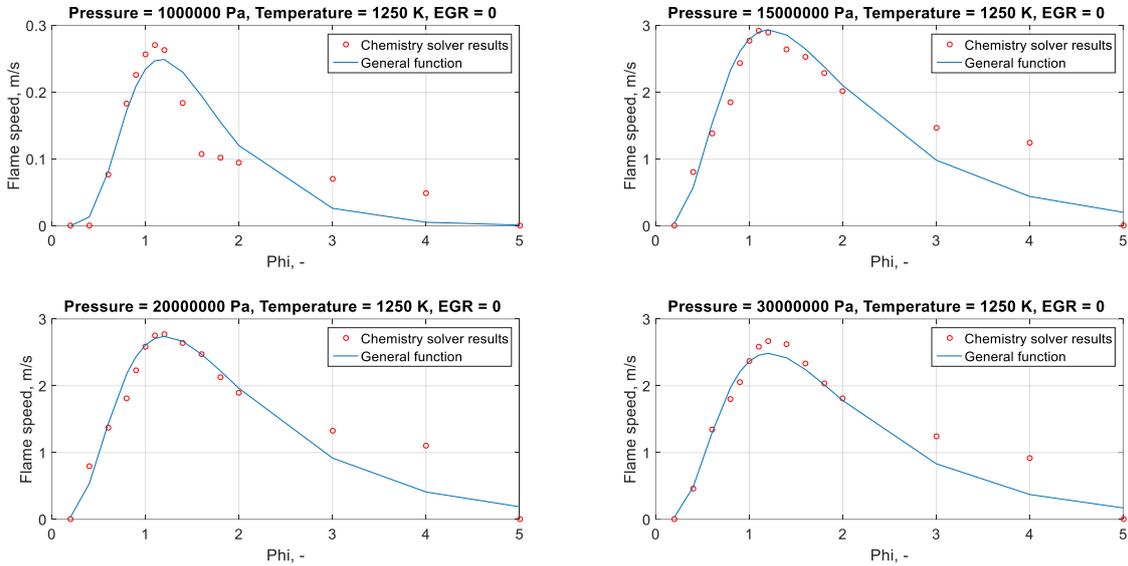
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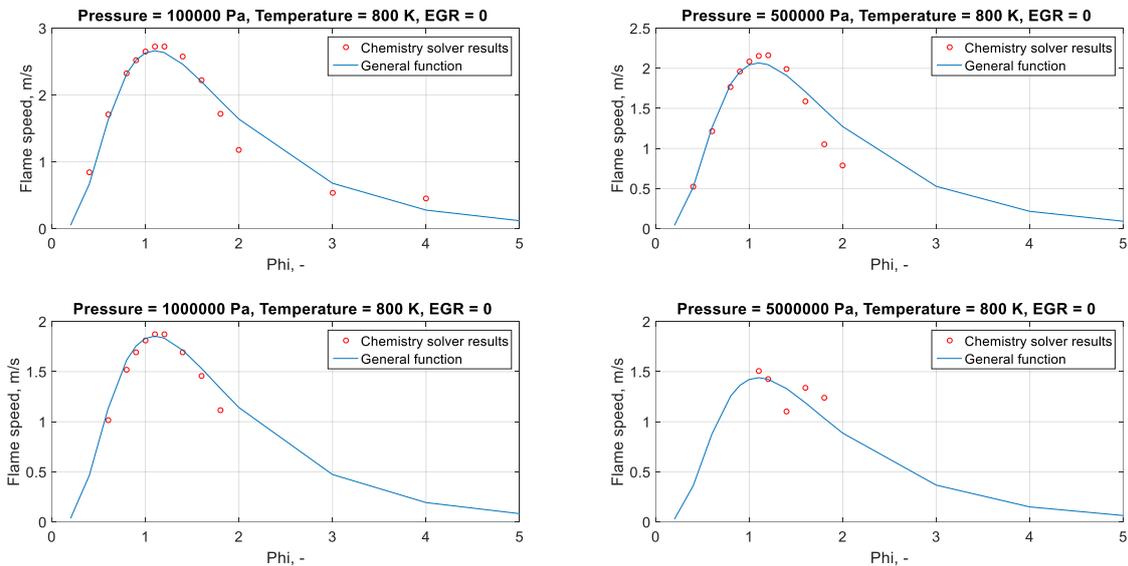


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323 Figure 7 Laminar flame speed results with the correlation functions at 300, 800 and 1250 K  
 324 and without EGR

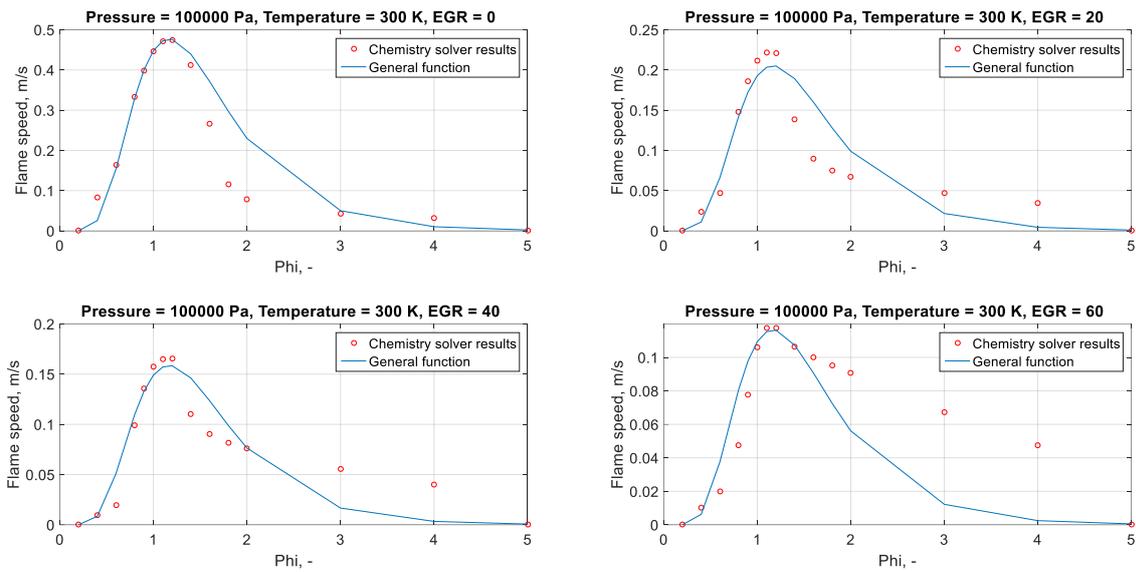


325  
 326 Figure 8 Calculated results with Gülder approach and laminar flame speed results with the  
 327 correlation function at 1250 K



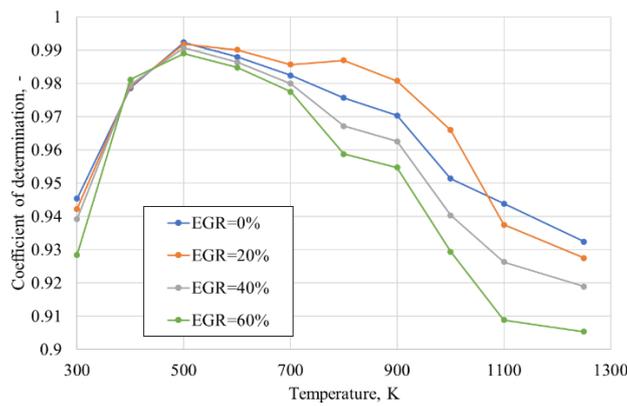
329  
 330 Figure 9 Chemistry solver results and laminar flame speed results with the correlation  
 331 function at 800 K

332



333  
 334  
 335 Figure 10 Chemistry solver results and laminar flame speed results with the correlation  
 336 function at different EGR values  
 337

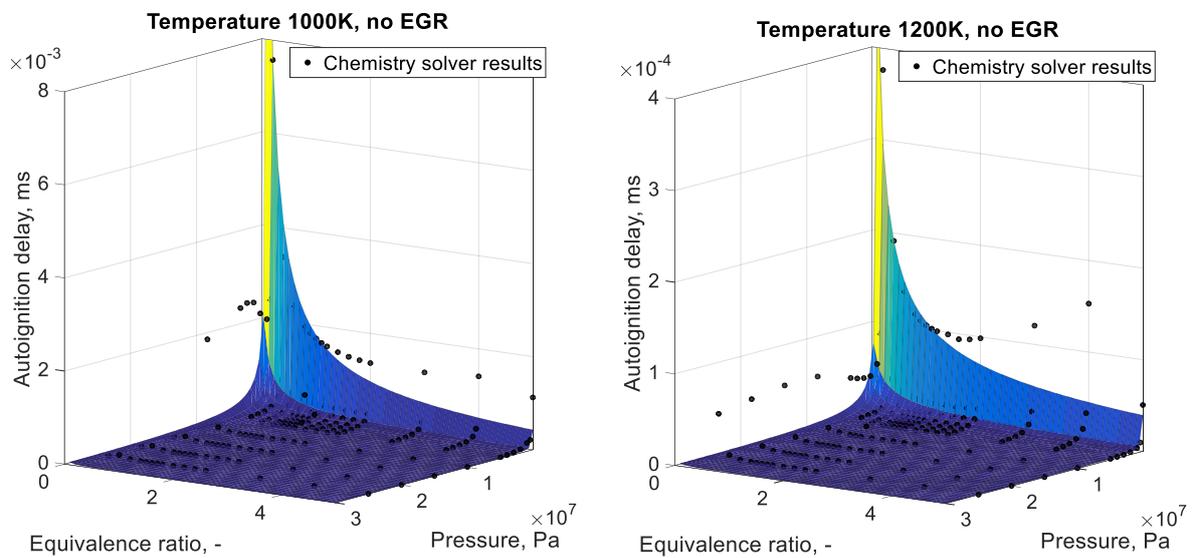
338 Figure 11 shows the coefficient of determination ( $R^2$ ) values between the chemistry solver  
 339 results and general function at different temperatures and EGR values. It can be seen that the best  
 340 agreement between chemistry solver results and general function is obtained around 500 K. the  
 341 correlation decreases markedly with the increase of EGR and at high temperatures.



342  
 343 Figure 11 Coefficient of determination values between chemistry solver results and general  
 344 function for different temperature and EGR values  
 345

346 **Pogreška! Izvor reference nije pronaden.** Figure 12 shows the calculated and tuned laminar  
 347 flame speed results with the correlation function in Equation (4) with Cai et al. chemical  
 348 mechanism. For most autoignition delay time representation, a logarithmic scale is used in order  
 349 to emphasize that the order of magnitude is sufficient for valid autoignition modeling. In Figure  
 350 12, the linear scale emphasizes a good agreement with the chemistry solver results at temperatures  
 351 1000 K and 1200 K.

352



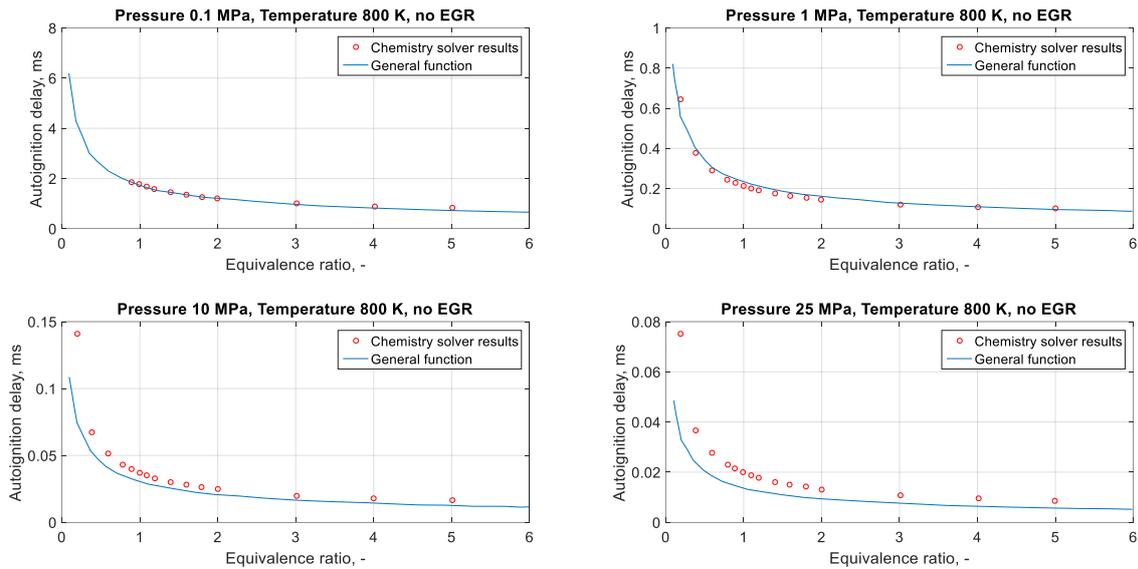
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354 Figure 12 Calculated (black dots) and autoignition timing results with the correlation functions  
 355 without EGR at 1000 and 1200 K

356

357 Figure 13 shows the same results as Figure 12 for 2D cuts at different pressure values. It can be  
 358 seen that the agreement between the calculated data and obtained results is better for the points  
 359 around the stoichiometric equivalence ratio and around the fuel-rich region. In contrast, additional  
 360 efforts are required for the lean air-fuel mixtures and the fuel-rich region at higher pressures.

361



362

363 Figure 13 Chemistry solver results and autoignition results with the correlation function

364

365 In section 4., the operating conditions and numerical setup for the calculation are presented,

366 for which the results are shown. The performed engine operating point features a multi-injection

367 strategy of four separate injections, where the OME-3 fuel was injected at 20 °C. Figure 14

368 compares the most detailed chemistry mechanism of OME-3 fuel, Cai et al., and ECFM-3Z

369 combustion model with implemented autoignition and laminar flame speed databases for two

370 operating injection strategies shown in Table 4. A good trend was achieved for the temperature

371 results, while the ignition timing was slightly delayed for the simulation of ECFM-3Z. That can

372 also be attributed to the autoignition parameter for ECFM-3Z calculation, which was not calibrated

373 but used as a default value of 1. The same ignition delay is observed for the rate of heat release

374 results, while the peak of released heat is achieved with the same value. As seen from RoHR

375 diagram, ECFM-3Z combustion is not so pronounced as with Cai et al. For the late-stage

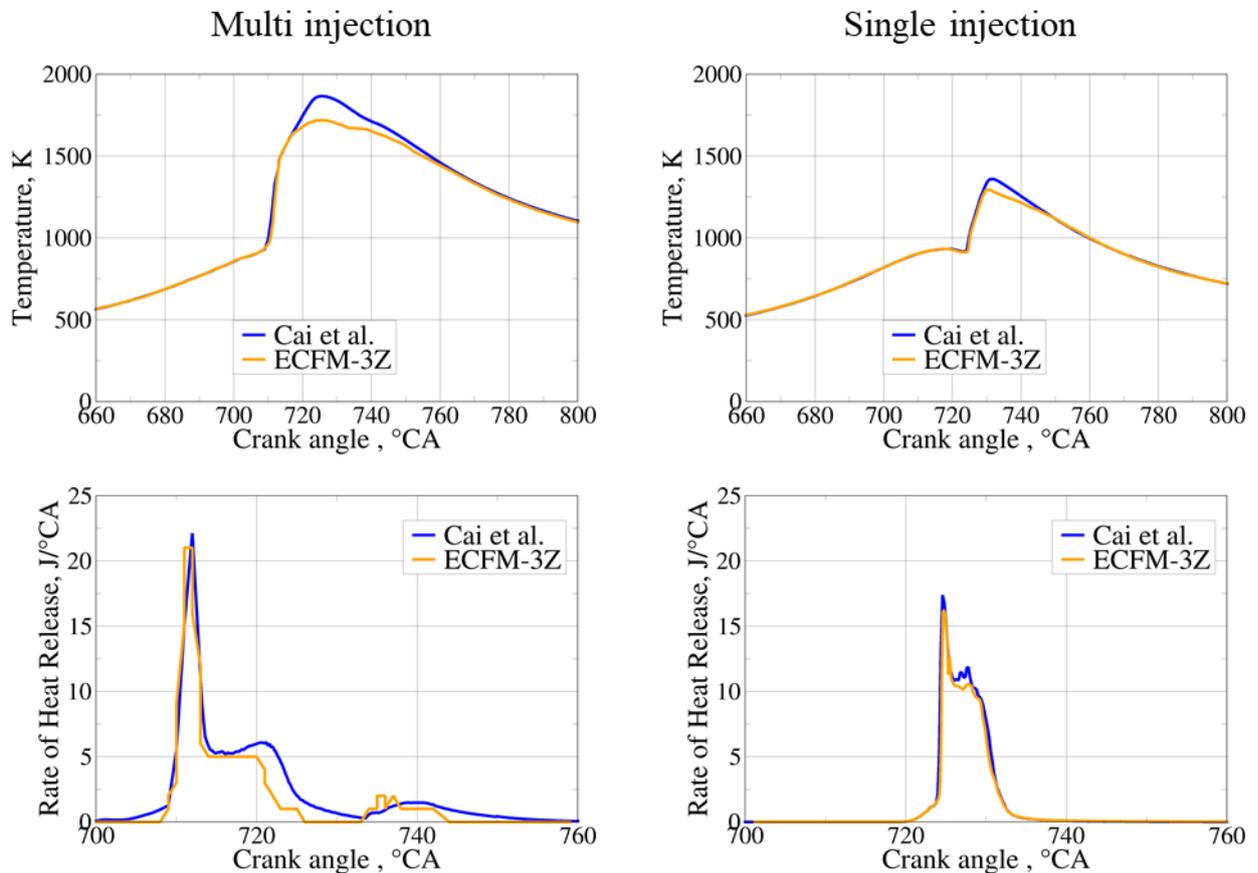
376 combustion, the biggest discrepancy is achieved, which can be mainly attributed to the simplified

377 chemistry in the combustion model does not account for such detailed carbon-based reactions. A

378 better agreement is reached for the single injection case than in a multi injection strategy with four

379 different injections, which calculates autoignition delay based on the whole chemistry reactions

380 rather than on interpolated conditions based on four parameters from the generated database. The  
381 ECFM-3Z in combination with the developed method for database generation of autoignition and  
382 laminar flame speed has correctly described the ignition of each injection and its ignition and  
383 combustion process with significantly simpler chemistry and decreased computational demand.  
384 The computational discrepancy between the ECFM-3Z model and Cai et al. mechanism can be  
385 attributed mainly to the simplified chemistry description in the ECFM-3Z model, which accounts  
386 for transport equations for a dozen chemical species. In contrast, Cai accounts for transport  
387 equations for 322 chemical species. Finally, the computational time was decreased approximately  
388 20 times with the ECFM-3Z model.



389  
390 Figure 14 Comparison of temperature and rate of heat release results between detailed  
391 chemistry mechanism by Cai et al. and ECFM-3Z combustion model

392

393        **6. CONCLUSIONS**

394        The procedure of general functions for the generation of databases required for combustion  
395        modeling in the coherent flame models is developed in this work. The procedure is general and  
396        applicable to every fuel, and this work was mainly focused on the generation of laminar flame  
397        speed and autoignition databases for OME-3 fuel. Additionally, the developed procedure showed  
398        a good potential for reducing the number of required grid points since a reasonable agreement can  
399        be achieved with a few calculated points around stoichiometric values of equivalence ratio. The  
400        procedure validation was performed on generated laminar flame speed and autoignition database  
401        for OME-3 fuel, where a good agreement was achieved compared to the available experimental  
402        results. For the engine operating cycles, verification was made compared to the most detailed  
403        chemistry mechanism available in the literature, Cai et al. The verification results showed a great  
404        agreement in the trend and autoignition timing between mean in-cylinder temperature and rate of  
405        heat release curves for both single and multi injection strategy. In combination with coherent flame  
406        models, the developed method represents a robust and computationally low demanding procedure  
407        for accurate ignition and combustion process calculations of new biofuels and e-fuels. Although  
408        not presented in this work, the procedure was also developed for fuel blends, dual fuel, and  
409        multiple fuel combustion, where the additional fuel composition parameter was added as the fifth  
410        grid parameter. Therefore, the future work investigates the obtained databases for dual fuel and  
411        the impact of generated databases on the whole operating cycle in CFD software.

412

413        **ACKNOWLEDGMENT**

414        This work was funded under the auspice of the European Regional Development Fund,  
415        Operational Programme Competitiveness and Cohesion 2014–2020, KK.01.1.1.04.0070.

416 The Authors would wish to thank LOGEsoft™ for providing the software license through  
417 Academic Partner Program and for their support.

418

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